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How Important are Financial Frictions in the U.S. and the Euro Area?
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# How Important are Financial Frictions in the U.S. and the Euro Area?* 

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#### Abstract

This paper aims to evaluate the importance of frictions in credit markets for business cycles in the U.S. and the Euro area. For this purpose, I modify the DSGE financial accelerator model developed by Bernanke, Gertler and Gilchrist (1999) and estimate it using Bayesian methods. The model is augmented with frictions such as price indexation to past inflation, sticky wages, consumption habits and variable capital utilization. My results indicate that financial frictions are relevant in both areas. Using the Bayes factor as criterion, the data favors the model with financial frictions both in the U.S. and the Euro area in five different specifications of the model. Moreover, the size of the financial frictions is larger in the Euro area.


Keywords: DSGE models; Bayesian estimation; financial accelerator JEL: C11, C15, E32, E40, E50, G10

[^0]
## 1 Introduction

The works of Bernanke and Gertler (1989) and Carlstrom and Fuerst (1997), where endogenous procyclical movements in entrepreneurial net worth magnify investment and output fluctuations, constitute the corner stone of most recent theoretical papers with financial frictions. ${ }^{1}$ Bernanke et al. (1996) develop the so-called financial accelerator, a mechanism based on information asymmetries between lenders and entrepreneurs that creates inefficiencies in financial markets, which affect the supply of credit and amplify business cycles. Specifically, during booms (recessions), an increase (fall) in borrowers' net worth decreases (increases) the borrowers' cost of obtaining external funds, which further stimulates (destimulates) investment amplifying the effects of the initial shock. ${ }^{2}$ The financial accelerator approach has become widely spread in the literature and many studies have introduced these types of frictions in DSGE models (Bernanke et al. (1999), henceforth BGG; Christiano et al. (2003)). The same idea has been used in growth models (Aghion et al. (2004), Aghion et al. (2003)) as well as in open economy models (Gertler et al. (2003), Gilchrist et al. (2002)).

Despite the ample theoretical work based on the financial accelerator, little has been done when it comes to the econometric estimation of these models. I only know of four papers estimating closed economy models with a financial accelerator. Christiano et al. (2003) estimate a DSGE model with a financial accelerator but they fix the parameters related to the financial frictions and use the same calibration as in BGG. They ask which shocks had a more important role in the Great Depression and if a different monetary policy could have moderated the crisis. Christensen and Dib (2004) estimate the standard BGG model for the U.S. using maximum likelihood and find evidence in favor of the

[^1]financial accelerator model. ${ }^{3}$ Meier and Muller (2005) use minimum distance estimation based on impulse responses to estimate a model with financial accelerator in the U.S., and find that financial frictions do not play a very important role in the model. ${ }^{4}$ Levin et al. (2004) use nonlinear least squares to estimate the structural parameters of a canonical debt contract model with informational frictions. Using microdata for 900 U.S. firms over the period 1997Q1 to 2003Q3, they reject the null hypothesis of frictionless financial markets.

Given the paucity of empirical work on the financial accelerator, the purpose of this paper is to answer two basic questions. First, I want to determine if a model with frictions in financial markets delivers a better description of the data than a model without such frictions, even if realistic frictions in goods and labor markets are added to the model. Specifically, I evaluate financial frictions as a source of propagation of shocks in the economy and not as a source of shocks. Second, I want to investigate if the magnitude of financial frictions is similar in the U.S. and the Euro area. One motivation for this is the existence of a common perception that financial markets are more developed in the U.S., and consequently, more efficient.

To answer these questions, I modify the standard BGG model and estimate it using Bayesian methods for U.S. and European data. Specifically, I extend the BGG model introducing price indexation to past inflation, sticky wages, consumption habits and variable capital utilization. One benefit of using Bayesian methods is that we can include prior information about the parameters, especially information about structural parameters from microeconomic studies. Another benefit is related to the fact that some parameters have a specific economic interpretation and a bounded domain, which can be incorporated in the priors.

[^2]The paper contributes to the existing literature in two main respects. First, it empirically investigates the importance of frictions in credit markets for business cycles both in the U.S. and the Euro area, and second, it uses Bayesian methods to estimates a DSGE model with a financial accelerator. ${ }^{5}$

The results indicate that financial frictions are relevant in both areas. Using the so-called Bayes factor as the evaluation criterion, I find that the data favors the model with financial frictions both in the U.S. and the Euro area. This is true for all five specifications of the model. Moreover, consistent with common perceptions, the size of financial frictions is larger in the Euro area.

The rest of the paper is organized as follows. In Section 2, I describe an alternative to the standard BGG model which incorporates other frictions to the economy while maintaining the existence of financial frictions. This model is going to be our benchmark model. Section 3 presents the estimation methodology while Section 4 presents the results. In Section 5, I discuss the results. Section 6 concludes.

## 2 The Model

The specification of the model follows the work of BGG who incorporate financial market frictions through a financial accelerator mechanism in a general equilibrium model. The main idea of the financial accelerator is that there exits a negative relationship between the external financial premium (the difference between the cost of funds raised externally and the opportunity cost of funds) and the net worth of potential borrowers. The intuition is that firms with higher leverage (lower net worth to capital ratio) will have a greater probability of defaulting and will therefore have to pay a higher premium. Since net worth is procyclical (because of the procyclicality of profits and asset prices), the external finance premium becomes countercyclical and amplifies business cycles through

[^3]an accelerator effect on investment, production and spending.
Moreover, and following the recent literature in DSGE models, I modify the original BGG model to improve its empirical performance by introducing a number of alternative real and nominal frictions commonly considered in the literature. More specifically, I allow for external habit formation in consumption, variable capital utilization and Calvo prices and wages with full indexation to previous period inflation. Christiano et al. (2005) show variable capital utilization and wage stickiness to be fundamental frictions for explaining inflation inertia and persistent, hump-shaped responses in output after policy shocks. The other frictions in the model help to account for the response of other variables such as consumption and investment. Then, I ask whether financial frictions are still empirically important.

Overall, the model is most similar to the one in Christiano et al. (2003), but with several differences. First, I do not include a banking sector. ${ }^{6}$ Second, the return on deposits received by households is in real terms, while in their paper it is nominal, which allows for a 'debt deflation' effect. Third, capital is produced with different technology functions: I follow BGG by assuming the existence of adjustment costs in the production of capital, rather than costs of changing the investment flow. Fourth, in my model, variable capital utilization arises because of higher depreciation rates, while in their model high capital utilization gives rise to higher cost in terms of goods. Last, I introduce external habit formation in consumption, while Christiano et al. (2003) use internal habits.

There are seven types of agents in the model: households, retailers, wholesale sector, capital producers, entrepreneurs, financial intermediaries and government. The following subsections describe the behavior of these agents.

[^4]
### 2.1 Households

Consider a continuum of monopolistically competitive individuals, indexed by $j$, whose total mass is normalized to unity. In each period, each of these households maximizes its expected lifetime utility choosing a final consumption good, $c_{t}^{j}$, nominal bonds issued by the government, $\mathrm{nb}_{t+1}^{j}$, and real deposits held at financial intermediates, $d_{t+1}^{j}$, which pay a real gross free risk rate $r_{t}$. Moreover, each household supplies differentiated labor services to the wholesale sector, $l_{t}^{j}$. Households discount the future at a rate $\beta$.

The representative household's period utility and budget constraint are

$$
U_{t}=\nu_{t}\left[\frac{1}{1-\sigma}\left(c_{t}^{j}-h c_{t-1}\right)^{1-\sigma}-\frac{\xi_{t}}{2}\left(l_{t}^{j}\right)^{2}\right]
$$

and

$$
\frac{\mathrm{nb}_{t+1}^{j}}{p_{t}}+d_{t+1}^{j}+c_{t}^{j}=\frac{w_{t}^{j}}{p_{t}} l_{t}^{j}+r_{t-1} d_{t}^{j}+r_{t-1}^{n} \frac{\mathrm{nb}_{t}^{j}}{p_{t}}-t_{t}+\operatorname{div}_{t},
$$

where $w_{t}^{j}$ is the nominal wage of household $j, p_{t}$ is the nominal level of prices, $t_{t}$ are lump sum taxes and $\operatorname{div}_{t}$ are dividends received from ownership of firms. $\nu_{t}$ and $\xi_{t}$ are shocks to consumer preferences for intertemporal consumption and leisure respectively, which follow $A R(1)$ processes with mean equal to one.

The introduction of external habit formation in consumption mainly helps to account for the gradual and hump-shaped response of consumption observed in the data after a monetary policy shock.

Households also supply differentiated labor services to the wholesale sector, where the labor aggregator has the Dixit-Stiglitz form

$$
l_{t}=\left[\int_{0}^{1}\left(l_{t}^{j}\right)^{1 /\left(\tau_{t}+1\right)} d j\right]^{\left(\tau_{t}+1\right)}
$$

and $\tau_{t}$ is a wage (net) mark up shock with mean $\tau$ (the steady state wage mark up). Firms minimize the cost of hiring a fixed amount of total labor given the different price of labor. The optimal demand for labor is

$$
l_{t}^{j}=\left(\frac{w_{t}}{w_{t}^{j}}\right)^{\left(\tau_{t}+1\right) / \tau_{t}} l_{t} .
$$

Integrating this equation and imposing the Dixit-Stiglitz aggregator for labor, we can express the aggregate wage index as

$$
w_{t}=\left[\int_{0}^{1}\left(w_{t}^{j}\right)^{-1 / \tau_{t}} d j\right]^{-\tau_{t}} .
$$

I assume that households can reset their wages with probability $(1-\vartheta)$ at each period. Whenever the household is not allowed to reset his wage contract, wages are set at $w_{t}^{j}=\pi_{t-1} w_{t-1}^{j}$, where $\pi_{t-1}$ is the gross inflation in the last period. According to Christiano et al. (2005), wage stickiness plays a crucial role in the performance of the model. The first-order condition with respect to wages is

$$
\begin{aligned}
& E_{t} \sum_{k=0}^{\infty}(\beta \vartheta)^{k} \nu_{t+k}\left(c_{t+k}^{j}-h c_{t-1+k}\right)^{-\sigma}\left(\frac{\widehat{w}_{t}^{j}}{p_{t+k}} l_{t+k}^{j}\left[\frac{1}{\tau_{t+k}}\right]\right) \\
= & E_{t} \sum_{k=0}^{\infty}(\beta \vartheta)^{k} \nu_{t+k} \xi_{t+k}\left(l_{t+k}^{j}\right)^{2}\left[\frac{\left(\tau_{t+k}+1\right)}{\tau_{t+k}}\right] .
\end{aligned}
$$

### 2.2 Final Good Sector

Firms in the final good sector produce a consumption good, $y_{t}$, in a perfectly competitive market, combining intermediate goods, $y_{t}^{s}$. The production function transforming intermediate goods into final output is the usual Dixit-Stiglitz aggregator given by

$$
y_{t}=\left[\int_{0}^{1}\left(y_{t}^{s}\right)^{1 /\left(\lambda_{t}+1\right)} d s\right]^{\left(\lambda_{t}+1\right)}
$$

where $\lambda_{t} \geq 0$ is a mark up shock with mean $\lambda$. Firms take prices as given and choose $y_{t}^{s}$ to minimize costs:

$$
\min _{y_{t}^{s}} \int_{0}^{1} p_{t}^{s} y_{t}^{s} d s
$$

subject to the Dixit-Stiglitz aggregator. The first-order conditions of this problem imply

$$
y_{t}^{s}=\left(\frac{p_{t}}{p_{t}^{s}}\right)^{\left(\lambda_{t}+1\right) / \lambda_{t}} y_{t}
$$

Integrating this equation and imposing the constraint, we can express the aggregate price index as

$$
p_{t}=\left[\int_{0}^{1}\left(p_{t}^{s}\right)^{-1 / \lambda_{t}} d s\right]^{-\lambda_{t}}
$$

### 2.3 Wholesale Sector

A variety of intermediate inputs are produced by a continuum of monopolistically competitive firms indexed by $s \in[0,1]$. Each firm hires the services of capital, $k_{t}^{s}$, and labor, $l_{t}^{s}$, to face the demand curve for its product. They rent capital from an entrepreneurial sector, which owns the capital stock.

Firms produce according to the following production function:

$$
y_{t}^{s}=a_{t}\left(k_{t}^{s}\right)^{\alpha}\left(l_{t}^{s}\right)^{1-\alpha},
$$

where $a_{t}$ is a productivity shock which follows a first order autoregressive process with mean one. Firms choose capital and labor to minimize their total costs, taking factor prices as given. The minimization problem can be written as

$$
\min _{l_{t}^{s}, k_{t}^{s}} \frac{w_{t}}{p_{t}} l_{t}^{s}+z_{t} k_{t}^{s},
$$

subject to the production function, and where $z_{t}$ is the real rental price of capital.
Moreover, wholesale firms have market power and can choose prices to maximize expected profits with probability $1-\theta$ in each period (Calvo, 1983). As in the case of wages, firms that cannot choose prices index their prices according to last period's inflation rate: $p_{t}^{s}=\pi_{t-1} p_{t-1}^{s}$.

For those firms that can choose prices, $\widehat{p}_{t}$, the optimal first-order condition is

$$
\begin{aligned}
& E_{t} \sum_{k=0}^{\infty}(\beta \theta)^{k} m_{t, t+k} y_{t+k}\left(1 / \lambda_{t+k}\right)\left[\frac{\widehat{p}_{t}}{p_{t-1} \pi_{t+k}}\right]^{-1 / \lambda_{t+k}} \\
= & E_{t} \sum_{k=0}^{\infty}(\beta \theta)^{k} m_{t, t+k} y_{t+k}\left(\lambda_{t+k}+1\right) / \lambda_{t+k} s_{t+k}\left[\frac{\widehat{p}_{t}}{p_{t-1} \pi_{t+k}}\right]^{-\left(\lambda_{t+k}+1\right) / \lambda_{t+k}}
\end{aligned}
$$

where $\beta^{k} m_{t, t+k}=\beta^{k} \frac{u_{c}(t+k)}{u_{c}(t)}$ is the stochastic discount factor between periods $t$ and $t+k$ and $s_{t}$ is the real marginal cost. Profits are distributed to households.

### 2.4 Capital Producers

The physical stock of capital, $\widetilde{k}_{t}$ (where the $t$ subscript indicates when capital is actually used), is produced by a continuum of competitive firms indexed by $j$. At the end
of each period, these firms produce new capital goods combining investment $i_{t}^{j}$, and the existing capital stock. Capital producers buy the undepreciated capital stock at the end of each period and after producing the new capital they sell it back to the entrepreneurs at a relative price $q_{t} .{ }^{7}$ I assume there to exist increasingly marginal adjustment costs in the production of capital: investment expenditures, $i_{t}^{j}$, deliver $\Phi\left(\frac{i_{t}^{j}}{\widetilde{k}_{t}^{j}}\right) \widetilde{k}_{t}^{j}$ new capitals goods. This generates a weaker response of investment to any shock and a relative price of capital different to one.

I assume investment decisions to be determined one period in advance, while the price of capital adjusts immediately after a shock. This assumption helps to account for a gradual response of investment to shocks affecting the real interest rate, a feature observed in the data. Capital producers solve the following problem:

$$
\max _{i_{t+1}^{j}} E_{t}\left[q_{t+1} \Phi\left(\frac{i_{t+1}^{j}}{\widetilde{k}_{t+1}^{j}}\right) \widetilde{k}_{t+1}^{j}-i_{t+1}^{j}\right]
$$

where near the steady state $\Phi>0, \Phi^{\prime}()>0,. \Phi^{\prime \prime}()<$.0 . I also assume that in steady state, the relative price of capital is one.

The law of motion of the aggregate capital stock is

$$
\widetilde{k}_{t+1}=\Phi\left(\frac{i_{t}}{\widetilde{k}_{t}}\right) \widetilde{k}_{t}+\left(1-\delta\left(u_{t}\right)\right) \widetilde{k}_{t}
$$

where $u_{t}$ is the rate of capital utilization ${ }^{8}, \delta\left(u_{t}\right) \in(0,1)$ is a convex depreciation function with $\delta^{\prime}()>$.0 , and $\delta^{\prime \prime}()>$.0 around the steady state. I choose the function $\delta\left(u_{t}\right)$ such that $\delta(0)=0, \delta(\infty)=1$ and in steady state $\delta(1)=\delta .{ }^{9}$

[^5]
### 2.5 Entrepreneurs and Financial Intermediaries

Entrepreneurs own the physical stock of capital, $\widetilde{k}_{t}$, and provide capital services, $k_{t}$. They finance capital purchases both with their own net worth and debt. Capital services are related to the physical stock of capital by

$$
k_{t}=u_{t} \widetilde{k}_{t} .
$$

Entrepreneurs are risk neutral and have finite horizons, being $\gamma$ the probability of survival to the next period. This assumption rules out the possibility of entrepreneurs accumulating enough wealth to be fully self-financed: part of their capital must be financed through bank loans with a standard debt contract.

At the end of period $t$, entrepreneurs decide how much to borrow. Then, at the beginning of period $t+1$, after observing all the shocks, they choose how intensely to use their capital.

### 2.5.1 Optimal Contract

As in BGG, the return on capital depends on both aggregate and idiosyncratic shocks. The ex post return on capital for entrepreneur $i$ is $\omega_{t+1}^{i} r_{t+1}^{k}$, where $\omega^{i}$ is an i.i.d. lognormal random variable with pdf $F(\omega)$ and mean one. ${ }^{10}$ The riskiness of entrepreneurs is determined by the variance of the idiosyncratic shock, $\sigma_{\omega}$. The average return of capital in the economy is

$$
r_{t+1}^{k}=\frac{u_{t+1} z_{t+1}+\left(1-\delta\left(u_{t+1}\right)\right) q_{t+1}}{q_{t}}
$$

Entrepreneurs finance their capital stock at the end of period $t$ with their own net worth at the end of the period, $n_{t+1}^{i}$, and banks loans, $b_{t+1}^{i}:{ }^{11}$

$$
q_{t} \widetilde{k}_{t+1}^{i}=n_{t+1}^{i}+b_{t+1}^{i} .
$$

[^6]The entrepreneur borrows from a financial intermediary that obtains its funds from households, with an opportunity cost equal to the riskless gross rate of return, $r_{t}$. In equilibrium, the intermediary holds a pooled, and perfectly safe, portfolio and the entrepreneurs absorb any aggregate risk.

Following a "costly state verification" problem of the type analyzed by Townsend (1979), in which lenders must pay a fixed auditing cost to observe an individual borrower's realized return, BGG assume monitoring costs to be a proportion $\mu$ of the realized gross payoff to the firms' capital ${ }^{12}$, i.e., monitoring costs equals $\mu \omega_{t+1}^{i} r_{t+1}^{k} q \widetilde{k}_{t+1}^{i}{ }^{13}$. When $\mu=0$, we are in the special case of frictionless financial markets.

The optimal contract will be incentive compatible, characterized by a schedule of state contingent threshold values of the idiosyncratic shock $\varpi_{t+1}^{i}$, such that for values of the idiosyncratic shock greater than the threshold, the entrepreneur is able to repay the lender, and for values below the threshold, the entrepreneur declares default and the lender obtains $(1-\mu) \omega_{t+1}^{i} r_{t+1}^{k} q_{t} \widetilde{k}_{t+1}^{i}$. Only one-period contracts between borrowers and entrepreneurs are feasible.

Under these assumptions, the optimal contract is chosen to maximize expected entrepreneurial utility, conditional on the expected return of the lender, for each possible realization of $r_{t+1}^{k}$, being equal to the riskless rate, $r_{t}$. The following two first-order conditions must hold in the optimal contract between entrepreneurs and banks ${ }^{14}$ :

$$
E_{t}\left\{\left(1-\Gamma\left(\varpi_{t+1}^{i}\right)\right) \frac{r_{t+1}^{k}}{r_{t}}+\lambda\left(\varpi_{t+1}^{i}\right)\left[\left(\Gamma\left(\varpi_{t+1}^{i}\right)-\mu G\left(\varpi_{t+1}^{i}\right)\right) \frac{r_{t+1}^{k}}{r_{t}}-1\right]\right\}=0
$$

and

$$
\left[\Gamma\left(\varpi_{t+1}^{i}\right)-\mu G\left(\varpi_{t+1}^{i}\right)\right] r_{t+1}^{k} q_{t} \widetilde{k}_{t+1}^{i}=r_{t}\left[q_{t} \widetilde{k}_{t+1}^{i}-n_{t+1}^{i}\right]
$$

where $\mu G\left(\varpi_{t+1}^{i}\right)=\mu \int_{0}^{\varpi_{\varpi+1}^{2}} \omega d F(\omega)$ is expected monitoring costs, $\Gamma\left(\varpi_{t+1}^{i}\right)=\left(1-F\left(\varpi_{t+1}^{i}\right)\right) \varpi_{t+1}^{i}+$ $G\left(\varpi_{t+1}^{i}\right)$ is the expected gross share of profits going to the lender, and $\lambda\left(\varpi_{t+1}^{i}\right)=$

[^7]$\frac{\Gamma^{\prime}\left(\varpi_{t+1}^{i}\right)}{\Gamma^{\prime}\left(\varpi_{t+1}^{i}\right)-\mu G^{\prime}\left(\varpi_{t+1}^{i}\right)}$.
From this first first-order condition, we see that when financial markets are frictionless, $\mu=0, \lambda\left(\varpi_{t+1}^{i}\right)=1$ and $E_{t} r_{t+1}^{k}=r_{t}$ : the ex-ante return on capital equals the risk free rate when there are no monitoring costs. The second first-order condition is related to the fact that the financial intermediary receives an expected return equal to the opportunity cost of its funds. In this case, the lender's expected return can simply be expressed as a function of the average cutoff value of the firm's idiosyncratic shock, $\varpi_{t+1}$.

Since the entrepreneur is risk neutral, he only cares about the mean return on his wealth. He guarantees the lender a return that is free of any systematic risk: conditional on $r_{t+1}^{k}$, he offers a state-contingent contract that guarantees the lender a return equal in expected value to the riskless rate.

From these two equations, aggregation is straightforward and it can be shown that capital expenditures by each entrepreneur $i$ are proportional to his net worth. Aggregate entrepreneurial net worth (in consumption units) at the end of period $t, n_{t+1}$ is given by

$$
n_{t+1}=\gamma\left\{r_{t}^{k} q_{t-1} \widetilde{k}_{t}-\left[r_{t-1}\left(q_{t-1} \widetilde{k}_{t}-n_{t}\right)+\mu \int_{0}^{\omega_{t}} \omega d F(\omega) r_{t}^{k} q_{t-1} \widetilde{k}_{t}\right]\right\}+w^{e},
$$

where $\gamma$ is the fraction of entrepreneurs surviving to the next period ${ }^{15}$, and $w^{e}$ are net transfers to entrepreneurs. At each period, a fraction $(1-\gamma)$ of new entrepreneurs enters the market receiving some transfers and the wealth of the fraction that did not survive is given to the government.

### 2.5.2 Optimal Capital Utilization Decision

After observing the shocks at the beginning of period $t+1$, entrepreneurs decide how intensively to use their capital. Higher capital utilization is costly because of higher depreciation rates. ${ }^{16}$ This is an important assumption because it allows for variable capital utilization, a relevant feature in the data. Entrepreneurs choose capital utilization,

[^8]$u_{t+1}$ to solve
$$
\max _{u_{t+1}}\left[\frac{u_{t+1} z_{t+1}+\left(1-\delta\left(u_{t+1}\right)\right) q_{t+1}}{q_{t+1}}\right] .
$$

### 2.6 Monetary and Fiscal Policy

The monetary authority conducts monetary policy by controlling the gross nominal interest rate, $r_{t}^{n}$. For convenience, I assume a cashless economy, but the monetary authority can set the interest rate directly in the interbank market. The central bank follows a Taylor type rule of the form

$$
r_{t}^{n}=H\left(r_{t-1}^{n} ; E_{t}\left(\pi_{t+1}\right) ; y_{t} ; \varepsilon_{t}^{r}\right),
$$

where $\varepsilon_{t}^{r}$ is a monetary policy shock and $\pi_{t+1}$ is inflation in $t+1$.
Government consumption expenditures, $g_{t}$, follow a first order autoregressive process. The government finances its expenditures by lump sum taxes, $t_{t}$, and nominal bonds, $\mathrm{nb}_{t+1} .{ }^{17}$

### 2.7 Competitive Equilibrium

In a competitive equilibrium all the above optimality conditions are satisfied. In addition, markets clear. The aggregate resource constraint is

$$
y_{t}=c_{t}+i_{t}+g_{t}+\mu \int_{0}^{\bar{\omega}_{t}} \omega d F(\omega) r_{t}^{k} q_{t-1} \widetilde{k}_{t} .
$$

Final goods are allocated to consumption, investment, government expenditure and monitoring costs ${ }^{18}$. Furthermore, credit markets clear and $b_{t}=d_{t}$.

### 2.8 The log-linearized model

To solve the model, I loglinearize the equilibrium conditions around their steady state values. The model can then be written in terms of three blocks of linear equations where

[^9]letters with a hat represent $\log$ deviations from the steady state at time $t$, and letters without a subscript represent the steady state values of the variables.

### 2.8.1 Equilibrium conditions

The loglinearized versions of aggregate demand and supply are

$$
\begin{equation*}
\widehat{y}_{t}=\frac{c}{y} \widehat{c}_{t}+\delta \frac{\widetilde{k}}{y} \widehat{i}_{t}+\frac{g}{y} \widehat{g}_{t}+\frac{\mu G(\varpi) r^{k} \widetilde{k}}{y}\left(\widehat{r}_{t}^{k}+\widehat{q}_{t-1}+\widehat{\widetilde{k}}_{t}\right)+\frac{\mu r^{k} G^{\prime}(\varpi) \widetilde{k} \varpi}{y} \widehat{\varpi}_{t} \tag{1}
\end{equation*}
$$

and

$$
\begin{equation*}
\widehat{y}_{t}=\widehat{a}_{t}+\alpha \widehat{k}_{t}+(1-\alpha) \widehat{l}_{t}, \tag{2}
\end{equation*}
$$

where $\delta$ is the steady state capital depreciation.
Next, I write the consumption Euler equation, equation (3); the arbitrage condition for nominal bonds, equation (4); and the law of motion of real wages, equation $(5)^{19}$ :

$$
\begin{gather*}
\widehat{c}_{t}=\frac{(1-h)}{\sigma(1+h)}\left(\widehat{\nu}_{t}-E_{t} \widehat{\nu}_{t+1}\right)+\frac{h}{(1+h)} \widehat{c}_{t-1}-\frac{(1-h)}{\sigma(1+h)} \widehat{r}_{t}+\frac{E_{t} \widehat{c}_{t+1}}{(1+h)},  \tag{3}\\
\widehat{r}_{t}^{n}=\widehat{r}_{t}+E_{t} \widehat{\pi}_{t+1}, \tag{4}
\end{gather*}
$$

$E_{t}\left\{\eta_{0} \widehat{w}_{t-1}^{r}+\eta_{1} \widehat{w}_{t}^{r}+\eta_{2} \widehat{w}_{t+1}^{r}+\eta_{3} \hat{\pi}_{t-1}+\eta_{4} \hat{\pi}_{t}+\eta_{5} \hat{\pi}_{t+1}+\eta_{6} \widehat{l}_{t}+\eta_{7}\left(\widehat{c}_{t}-h \widehat{c}_{t-1}\right)+\eta_{8} \widehat{\xi}_{t}+\eta_{9} \widehat{\tau}_{t}\right\}=0$,
where $b_{w}=[(\tau+1)+\tau] /[(1-\vartheta)(1-\beta \vartheta)]$ and

$$
\eta=\left(\begin{array}{c}
b_{w} \vartheta \\
-b_{w}\left(1+\beta \vartheta^{2}\right)+(\tau+1) \\
\beta \vartheta b_{w} \\
b_{w} \vartheta \\
-\vartheta b_{w}(1+\beta) \\
b_{w} \beta \vartheta \\
\tau \\
\tau \sigma(1-h)^{-1} \\
\tau \\
\tau \frac{\tau}{\tau+1}
\end{array}\right)=\left(\begin{array}{c}
\eta_{0} \\
\eta_{1} \\
\eta_{2} \\
\eta_{3} \\
\eta_{4} \\
\eta_{5} \\
\eta_{6} \\
\eta_{7} \\
\eta_{8} \\
\eta_{9}
\end{array}\right) .
$$

[^10]These three equations are derived from the households' first-order conditions. $\tau$ is the net wage mark up in steady state; $\widehat{\nu}_{t}$ is the preference shock, and $\widehat{\xi}_{t}$ is the labor supply shock.

The demand for labor and capital in the wholesale sector, where factor prices are equal to marginal productivity plus real marginal cost, $\widehat{s}_{t}$, are given by

$$
\begin{equation*}
\widehat{y}_{t}-\widehat{l}_{t}+\widehat{s}_{t}=\widehat{w}_{t}^{r} \tag{6}
\end{equation*}
$$

and

$$
\begin{equation*}
\widehat{s}_{t}+\widehat{y}_{t}-\widehat{k}_{t}=\widehat{z}_{t} . \tag{7}
\end{equation*}
$$

A Phillips curve can be derived from the wholesale sector optimization problem for prices, where $(1-\theta)$ is the probability of adjusting prices and $\lambda$ is the net price mark up in steady state:

$$
\begin{equation*}
\widehat{\pi}_{t}=\frac{\widehat{\pi}_{t-1}}{(1+\beta)}+\frac{\beta}{(1+\beta)} E_{t} \widehat{\pi}_{t+1}+\frac{(1-\theta)(1-\beta \theta)}{(1+\beta) \theta} \widehat{s}_{t}+\frac{(1-\theta)(1-\beta \theta)}{(1+\beta) \theta} \frac{\lambda}{(\lambda+1)} \widehat{\lambda}_{t} . \tag{8}
\end{equation*}
$$

Capital producers' optimality condition is

$$
\begin{equation*}
E_{t} \widehat{q}_{t+1}+\varphi\left[\widehat{i}_{t+1}-\widehat{\widetilde{k}}_{t+1}\right]=0 \tag{9}
\end{equation*}
$$

This equation links asset prices and investment, where $\varphi=\Phi^{\prime \prime}\left(\frac{i}{\tilde{k}}\right)\binom{i}{\bar{k}}$ is the elasticity of the price of capital with respect to the investment-capital ratio.

The equilibrium conditions of the entrepreneurs are

$$
\begin{gather*}
E_{t} \widehat{r}_{t+1}^{k}-\widehat{r}_{t}=E_{t} \widehat{\varpi}_{t+1} \varpi \frac{r^{k}}{r}(1-\Gamma(\varpi))\left[\frac{\Gamma^{\prime \prime}(\varpi)}{\lambda(\varpi) \Gamma^{\prime}(\varpi)}-\frac{\Gamma^{\prime \prime}(\varpi)}{\Gamma^{\prime}(\varpi)}+\frac{\mu G^{\prime \prime}(\varpi)}{\Gamma^{\prime}(\varpi)}\right],  \tag{10}\\
{\left[(1-F(\varpi))-\mu G^{\prime}(\varpi)\right] \frac{\widetilde{k}}{n} \frac{r^{k}}{r} \varpi \widehat{\varpi}_{t+1}+\left[\frac{\widetilde{k}-n}{n}\right]\left(\widehat{r}_{t+1}^{k}-\widehat{r}_{t}\right)=\widehat{\widetilde{k}}_{t+1}+\widehat{q}_{t}-\widehat{n}_{t+1},}  \tag{11}\\
\widehat{k}_{t}=\widehat{u}_{t}+\widehat{\widetilde{k}}_{t}, \tag{12}
\end{gather*}
$$

and

$$
\begin{equation*}
\widehat{z}_{t+1}=\frac{\delta^{\prime \prime}(1)}{\delta^{\prime}(1)} \widehat{u}_{t+1}+\widehat{q}_{t+1} . \tag{13}
\end{equation*}
$$

Equations (10) and (11) are the first-order conditions of the optimal lending contract. ${ }^{20}$ Equation (12) relates capital services to the capital stock, while equation (13) is the optimality condition for capital utilization.

The loglinearized return on capital is

$$
\begin{equation*}
\widehat{r}_{t+1}^{k}=\frac{z}{r^{k}} \widehat{z}_{t+1}+\frac{(1-\delta)}{r^{k}} \widehat{q}_{t+1}-\widehat{q}_{t} . \tag{14}
\end{equation*}
$$

Equations (15) and (16) are the law of motion of net worth and capital respectively:

$$
\widehat{n}_{t+1}=\gamma\left\{\begin{array}{c}
\left(\frac{\widetilde{k}-\mu G(\varpi) \widetilde{k}}{n}\right) r^{k} \widehat{r}_{t}^{k}+\left(\frac{r^{k} \widetilde{k}-\widetilde{k} r-\mu G(\varpi) r^{k} \widetilde{\widetilde{k}}}{n}\right) \widehat{q}_{t-1}+\left(\frac{r^{k}-r-\mu G(\varpi) r^{k}}{n}\right) \widetilde{\widetilde{k}}_{t}  \tag{15}\\
-\left(\frac{\widetilde{k}-n}{n}\right) r \widehat{r}_{t-1}+r \widehat{n}_{t}-\left(\frac{\mu r^{k} G_{w} \widetilde{k}}{n}\right) \varpi \widehat{\varpi}_{t}
\end{array}\right\}
$$

and

$$
\begin{equation*}
\widehat{\widetilde{k}}_{t+1}=\delta \widehat{i}_{t}+(1-\delta) \widehat{\widetilde{k}}_{t}-\delta^{\prime}(1) \widehat{u}_{t} . \tag{16}
\end{equation*}
$$

### 2.8.2 Monetary policy rule

The loglinearized monetary policy rule is

$$
\begin{equation*}
\widehat{r}_{t}^{n}=\rho^{r} \widehat{r}_{t-1}^{n}+\left(1-\rho^{r}\right)\left(\gamma^{\pi} E \widehat{\pi}_{t+1}\right)+\left(1-\rho^{r}\right)\left(\gamma^{y} \widehat{y}_{t}\right) / 4+\widehat{\varepsilon}_{t}^{r} . \tag{17}
\end{equation*}
$$

### 2.8.3 Shock Process

There exist seven shocks in the model:

$$
\begin{align*}
& \widehat{\varepsilon}_{t}^{r}=\varepsilon_{t}^{r},  \tag{18}\\
& \widehat{\lambda}_{t}=\varepsilon_{t}^{\lambda}, \tag{19}
\end{align*}
$$

[^11]and
$$
\widehat{n}_{t+1}=\gamma R\left\{\left(\frac{\widetilde{K}}{N}\right) \widehat{r}_{t}^{k}-\left(\frac{\widetilde{K}-N}{N}\right) \widehat{r}_{t-1}+\widehat{n}_{t}\right\}
$$

The first equation shows that without monitoring costs, the ex-ante risk premium is zero.

$$
\begin{gather*}
\widehat{\tau}_{t}=\varepsilon_{t}^{\tau},  \tag{20}\\
\widehat{\xi}_{t}=\rho^{\xi} \widehat{\xi}_{t-1}+\varepsilon_{t}^{\xi},  \tag{21}\\
\widehat{\nu}_{t}=\rho^{\nu} \widehat{\nu}_{t-1}+\varepsilon_{t}^{\nu},  \tag{22}\\
\widehat{g}_{t}=\rho^{g} \widehat{g}_{t-1}+\varepsilon_{t}^{g}, \tag{23}
\end{gather*}
$$

and

$$
\begin{equation*}
\widehat{a}_{t}=\rho^{a} \widehat{a}_{t-1}+\varepsilon_{t}^{a} \tag{24}
\end{equation*}
$$

where $\varepsilon_{t}^{i}$ are white noise shocks affecting the economy.
Equations (18)-(20) are the monetary policy, price mark up and wage mark up shocks. I specify these shocks as white noise shocks. The rest of the shocks in the model, to labor supply, preferences, government spending and technology follow a first-order autoregressive process. I choose this specification for the shocks to avoid identification problems.

### 2.8.4 Solution Method

To solve the model, I use the method described in Sims (2000) and his matlab code gensys.m. The loglinearized model can be written as

$$
\Gamma_{0} X_{t}=\Gamma_{1} X_{t-1}+\Psi V_{t}+\Pi W_{t}
$$

where $V_{t}$ is a vector of exogenous random disturbances, and $W_{t}$ is a vector of expectational errors with mean zero.

### 2.9 The Standard BGG Model

When estimating the model, I start out with the standard BGG model and then add four frictions not present in that model: price indexation to past inflation, sticky wages, external habit formation in consumption and variable capital utilization. I add these frictions cumulatively, one by one. Once all four frictions have been added, I obtain the
benchmark model described earlier in this section. For each of the five versions, I estimate the model both with and without monitoring costs.

The intention of this exercise is to check the robustness of the results when other commonly used frictions are included. Moreover, we want to see which frictions are more relevant to fit the data.

To fix ideas, I will next describe the four main differences between the benchmark model described in this section and the standard BGG model. ${ }^{21}$

First, in the standard BGG model, firms that are not allowed to reoptimize prices do not index their prices to past inflation. Equation (8) becomes

$$
\widehat{\pi}_{t}=\beta E_{t} \widehat{\pi}_{t+1}+\frac{(1-\theta)(1-\beta \theta)}{(1+\beta) \theta} \widehat{s}_{t}+\frac{(1-\theta)(1-\beta \theta)}{(1+\beta) \theta} \frac{\lambda}{(\lambda+1)} \widehat{\lambda}_{t},
$$

where inflation does not depend on past inflation as in the benchmark model and I have added a price mark up shock. I include price indexation in the benchmark model since this introduces a lagged inflation term component in inflation which generates inflation inertia, an aspect observed in the data.

Second, in the standard BGG model, wages are flexible, and equation (5) becomes the standard consumer first-order condition with respect to labor:

$$
\widehat{w}_{t}^{r}-\sigma(1-h)^{-1}\left(\widehat{c}_{t}-h \widehat{c}_{t-1}\right)=\widehat{\xi}_{t}+\widehat{l}_{t}+\frac{\tau}{\tau+1} \widehat{\tau}_{t}
$$

where I have added the existence of wage mark up shocks.
Third, households do not exhibit external consumption habits, $h=0$ and equation (3) becomes the standard Euler equation plus a preference shock:

$$
\widehat{c}_{t}=\frac{1}{\sigma}\left(\widehat{\nu}_{t}-E_{t} \widehat{\nu}_{t+1}\right)-\frac{1}{\sigma} \widehat{r}_{t}+E_{t} \widehat{c}_{t+1} .
$$

The introduction of consumption habits mainly helps to account for the gradual and hump-shaped response of consumption observed in the data.

[^12]Fourth, since there is not variable capital utilization, equation (13) is replaced by $\widehat{u}_{t}=0$ and the depreciation rate is constant. Introducing variable capital utilization helps to offset the fluctuations in labor productivity and affects the marginal cost, which is reflected in a more gradual response of prices.

The rest of the equations are those presented in Section 2.8.

## 3 Methodology for Estimation and Model Evaluation

The model has a total of 30 free parameters. Seven of these are calibrated to their steady state values, as they cannot be identified from the detrended data. The steady state rate of depreciation of capital $\delta$ is set equal to 0.025 , which corresponds to an annual rate of depreciation of ten percent. The discount factor $\beta$ is set at 0.99 , which corresponds to an annual real rate in steady state of four percent. The steady state share of government spending was set equal to 19.5 percent ${ }^{22}$. The parameter of the CobbDouglas function, $\alpha$, was set equal to 0.33 , while the steady state price mark up, $\lambda$, was set at 20 percent. These values imply steady state consumption and investment ratios of 60.9 and 19.6 percent in models without financial frictions ${ }^{23}$. Moreover, the steady state wage mark up, $\tau$, was set equal to five percent, and the steady state probability of default, $F(\varpi)$, equal to three percent per year, the same value as BGG.

The remaining 23 parameters are estimated using Bayesian procedures. The advantage of Bayesian estimation relative to maximum likelihood (the only realistic alternative), is that the solution of the model implies many restrictions and boundary values for the parameters which are difficult to impose using maximum likelihood. Besides, using Bayesian methods also makes it possible to formally incorporate our beliefs about the

[^13]parameters.
I start by solving the model for an initial set of parameters. Then, the Kalman Filter is used to calculate the likelihood function of the data (for given parameters). Combining prior distributions with the likelihood of the data gives the posterior kernel which is proportional to the posterior density. Since the posterior distribution is unknown, we use Markov Chain Monte Carlo (MCMC) simulation methods to conduct inference about the parameters.

To check convergence, I run different chains starting from dispersed points. Each set of estimates is based on two different chains starting from the mode of the posterior plus-minus two standard deviations, with a total of 100000 draws in each simulation and a burn-in period of 50.000 . Convergence was monitored calculating the potential scale reduction, $\widehat{R}$, as described in Gelman et al. (2004), which declines to 1 as convergence is achieved. If the potential scale reduction is high, one should proceed with further simulations to improve inference. This ratio was computed for all parameters.

### 3.1 Data

The data used for the estimation corresponds to seven variables of the model: real output, real consumption, real investment, hours worked, nominal interest rate, inflation and real wages. ${ }^{24}$ In all the cases, I use quarterly detrended data. For the U.S., the data covers the period 1980Q1-2004Q1 ${ }^{25}$, while for the Euro area, it covers the period

[^14]
### 3.2 Prior Distribution

All prior distributions of the parameters were selected from the normal, beta, gamma and uniform distributions, depending on the different supports and characteristics of the parameters. The prior distributions are the same for the U.S. and the Euro area and are shown in Table 1.

Many of the priors are standard and follow the literature (Smets and Wouters (2004), Adolfson et al. (2004)). The relative risk aversion coefficient, $\sigma$, has a normal distribution with mode one; the habit persistence parameter, $h$, has a beta distribution with mode 0.70. The parameters determining prices and wages follow a beta distribution. The modes of the Calvo parameters $\theta$ and $\vartheta$, the probability of not adjusting prices and wages, were set equal to 0.70 , so that, on average, prices and wages adjust every ten months.

Some of the parameters are particular to the way I capture some frictions in the model. This is the case of the elasticity of the price of capital with respect to the investment-capital ratio, $\varphi$. There is no consensus about this parameter: BGG set it equal to -0.25 while King and Wolman (1996) use a value of -2 based on estimations of Chirinko (1993). Since there is not enough information about this parameter, I use a uniform prior distribution between -1 and 0 . The prior for $\delta^{\prime \prime} / \delta^{\prime}$ is a gamma distribution with mode equal to one, following the calibrations of Baxter and Farr (2001).

[^15]Other non standard parameters in the model are those related to the financial frictions. Following BGG, the prior for monitoring costs, $\mu$, was assumed to be beta distributed with mode equal to 0.12 . The fraction of entrepreneurs surviving to the next period, $\gamma$, has a beta distribution with mode 0.975 which implies that on average, entrepreneurs live ten years. Finally, the prior for the steady state external risk premium (the difference between the cost of funds raised externally and the opportunity cost of funds), $r^{k}-r$, was set gamma distributed with a mode 0.005 , which corresponds to an annual two percent risk premium as in BGG.

The priors for the parameters of the monetary policy rule are based on the estimates of Clarida et al. (2000) for the post-82 period. The long run coefficients on inflation and output, $\gamma^{\pi}$ and $\gamma^{y}$, are normally distributed with mode 1.5 and 0.5 respectively. The interest rate smoothing parameter, $\rho_{r}$, follows a beta distribution with mode 0.85 .

Regarding the shocks affecting the economy, the autoregressive coefficients have a beta distribution with mode 0.85 , while the standard deviations for the shocks follow a gamma distribution with mode 0.01 for the monetary, technology and government shocks, and 0.10 for the other shocks.

### 3.3 Model Comparison

To compare pairwise the performance of the different models, I calculate the Bayes factor, which is defined as the ratio of the marginal data densities between model $i$ and $j$. Jeffreys (1961) suggested rules of thumb to interpret the Bayes factor as follows:

| $B_{i j}<1$ | support for model $j$ |
| :---: | :--- |
| $1<B_{i j}<3$ | very slight evidence against model $j$ |
| $3<B_{i j}<10$ | slight evidence against model $j$ |
| $10<B_{i j}<100$ | strong evidence against model $j$ |
| $B_{i j}>100$ | decisive evidence against model $j$ |

One problem with this approach is how to compute the marginal likelihood, which is obtained by integrating the sample density with respect to the prior distribution. In
particular, I use the modified harmonic mean to approximate the marginal likelihood.

## 4 Results

I first present the results for the U.S. and then for the Euro area. To check the relevance of the financial accelerator mechanism, I start estimating the standard BGG model. Then, I add, one at a time, price indexation to past inflation, sticky wages, consumption habits and variable capital utilization. I reestimate the parameters of each alternative model with and without financial frictions. This allows me to test for the financial accelerator mechanism using the Bayes factor as the evaluation criterion.

### 4.1 U.S.

### 4.1.1 Frictions in the U.S.

In Table 2, I report the posterior mean of the parameters and the marginal data density for alternative models using U.S. data. In all specifications of the model, the Bayes factor is greater than 100, which is decisive evidence against the model without a financial accelerator. This extends the findings by Christensen and Dib (2004) who only estimate the standard BGG model with maximum likelihood and provide evidence in favor of a financial accelerator. In particular, the table shows that the estimated mean of monitoring costs in the benchmark case is twelve percent. This result is in line with the results of Levin et al. (2004). Using microdata for 900 U.S. firms over the period 1997Q1 to 2003Q3, they estimate that time varying monitoring cost moved between eight and sixteen percent between 1997 and 1999. When they smooth through a spike in 1998Q4, the average monitoring costs during this period is close to twelve percent of the realized gross payoff to the firms' capital. After the fall of the stock market in 2000, monitoring costs went up to reach values as high as forty percent, and then declined again in 2003.

Table 2 also indicates that the size of monitoring costs decreases once we introduce
other frictions to the standard BGG model. In the standard BGG case, monitoring costs are almost twice as large as in the benchmark model. The intuition is that high monitoring costs are necessary for the standard BGG model to capture the dynamics of the data. Once other frictions are introduced, however, the data does not require such large financial frictions. ${ }^{27}$

It is important to mention than when we add price indexation and sticky wages, the data marginal density decreases. This is probably due to the fact that in both cases I am imposing full indexation to past inflation. Smets and Wouters (2004) estimate that for the U.S., the mean degree of price and wage indexation is 0.34 and 0.75 respectively. In the model, I am constraining these parameters to be equal to unity in order to reduce the number of parameters to estimate.

### 4.1.2 Parameter Estimates for the U.S.

I will now only focus on the benchmark model, which includes all the frictions. Table 1 reports the mean, median and the 5 th and 95 th percentile of the posterior distribution of the benchmark model for U.S. data. Plotting the path of the different parameters along the chain, as well as the value of the posterior likelihood function, we see convergence to a stationary distribution. Moreover, when I calculate the potential scale reduction, this is confirmed. The only parameter which presents some doubts is the variance of the wage mark up shocks, $\sigma^{\tau}$. However, relatively small changes in the value of this parameter does not affect the properties of the model since it is multiplied by a very small number in the solution.

The estimated posterior mean of the risk premium in steady state, $r k-r$, implies an annual premium of 2.4 percent, which is in line with the value used by BGG and Christiano et al. (2003). Together with other parameters, this value implies that the

[^16]investment and consumption output ratio in steady state are 17 and 63 percent respectively. Moreover, the fraction of GDP used in bankruptcy costs is around 0.4 percent, and the mean for the fraction of entrepreneurs who survive, $\gamma$, is 0.99 , implying an average duration of entrepreneurs of 27 years. ${ }^{28}$

Table 1 indicates that the four autoregressive shocks affecting the economy present a high persistence, compared to the priors.

The coefficients describing consumer preferences do not differ substantially from the priors. The mean of risk aversion is 1.1 rather than one as the prior, and the habit persistence parameter has a posterior mean of 0.60 as compared to the prior mean of 0.70 .

The posterior mean of $\theta$ implies that prices adjust on average once every fourteen months. This result implies more flexible prices than Smets and Wouters (2004). The same occurs with wages, where the average duration of contracts if estimated at only four months. Both the elasticity of capital price with respect to the investment capital ratio, $\varphi$, and the variable depreciation parameter, $\delta^{\prime \prime} / \delta^{\prime}$, have a similar posterior mean as the prior: -0.47 and 1.02 respectively.

Concerning the coefficients in the central bank instrument rule, all coefficients differ from the estimates of Clarida et al. (2000). The coefficient on future inflation, $\gamma^{\pi}$, is higher while the coefficient on output, $\gamma^{y}$, and the interest rate smoothing parameter, $\rho_{r}$, are lower.

In the case of the same model but without monitoring costs (no financial accelerator), the estimation is robust for most of the parameters. However, the estimates of two parameters differ considerably. This is the case of the elasticity of the price of capital, $\varphi$, and the entrepreneurs' rate of survival, $\gamma$. Both these parameters are higher in the model with financial frictions. A possible explanation is that in a model with financial

[^17]accelerator investment reacts more to shocks, which requires higher adjustment costs to match the dynamics of investment in the data. This implies that monitoring costs are not relevant because the model cannot explain investment behavior, but because monitoring costs help to explain other variables. Moreover, to ensure that self-financing never occurs, estimates of the probability of survival are lower in a frictionless credit market model. In addition, monetary policy reacts slightly stronger to output in the case with financial frictions which dampens the amplification of output fluctuations caused by the financial accelerator.

To assess the model fit, Figure 5 shows the actual and one-side Kalman filter fitted data evaluated at the posterior mean for the benchmark model with and without monitoring costs. The model with financial frictions seems to better fit the data, which is in accordance to the Bayes factor criterion.

### 4.2 Euro Area

### 4.2.1 Frictions in the Euro Area

In Table 3, I report the posterior mean and the marginal data density for alternative models using European data. Also for European data, the Bayes factor is greater than 100 in all five different specifications, which clearly favors a model with monitoring costs. In the benchmark case, the posterior mean of monitoring costs is 18 percent, fifty percent higher than the cost estimated for the U.S. This number is higher in almost all other specifications of the model, reaching values as high as 52 percent in the model with price indexation and sticky wages. Moreover, for each model, the estimated mean of monitoring costs is higher than in the U.S.

Considering the other frictions in the model, price indexation and variable capital utilization seem to be the most important ones. ${ }^{29}$

[^18]
### 4.2.2 Parameter Estimates for the Euro Area

Table 1 also reports the mean, median and the 5 th and 95 th percentile of the posterior distribution of the benchmark model for European data. The value of the potential scale reduction indicates some convergence problems for the parameters governing variable capital depreciation and preference shocks. However, small changes in the value of these parameters do not affect the properties of the model when the impulse response functions are plotted.

The posterior distribution of the parameters using European data is in general very similar to that of the U.S. This indicates that the shocks driving the economy and the transmission mechanisms in the two areas are not too different. However, some parameters display more distinct differences.

The fact that monitoring costs are larger in the Euro area drives up the external risk premium: in the Euro area, the posterior mean of the annual risk premium is 3.6 percent in steady state. This implies that in steady state, the investment and consumption ratio to output are 15.6 and 64.3 percent, respectively, and that the fraction of GDP used in bankruptcy cost is 0.6 percent.

Concerning the size of the shocks affecting both economies, monetary shocks are smaller in the Euro area: the posterior mean value for the standard deviation of monetary shocks is 145 basis points (annual) in the U.S., but only 92 basis points in the Euro area. This difference in monetary policy shocks among the U.S. and the Euro area have also been documented, among others, in Angeloni et al. (2003) and Smets and Wouters (2004). Another difference is that preference shocks are larger in the Euro area, while wage mark up shocks are smaller. When it comes to persistence, while technology shocks are slightly more persistent in the Euro area, government spending shocks are less persistent.

The mean of risk aversion in the Euro area is 1.2, which is higher than in the U.S. On the other hand, the parameter of consumption habit formation is smaller in the Euro area, and around 0.50 .

Concerning price stickiness, prices adjust every six quarters on average. This implies that prices are more sticky in the Euro area, consistent with Peerman and Smets (2001), who find that the impact on prices after a monetary shock is faster in the U.S. Moreover, wage behavior is very similar to the U.S.: wages change every four months on average.

The elasticity of the price of capital with respect to the investment capital ratio, $\varphi$, is larger in Europe, with a mean value of -0.97 . Given larger monitoring costs in the Euro area, the model requires higher adjustment costs in investment to dampen the response of investment after a shock. In the model, these two effects offset each other and investment responds similarly in the U.S. and the Euro area after most of the shocks..

The coefficients in the monetary rule are similar in both areas, and different from the prior, suggesting that both areas have responded in a similar way to expected inflation and output in the last twenty years. As in the case of the U.S., the response of the interest rate to output is stronger in the model with financial frictions.

In Figure 6, I plot the actual and one-side Kalman filter fitted data of the benchmark model with and without monitoring costs. The figure shows that the model with a financial accelerator slightly better represents the actual data.

## 5 Discussion

The results show that frictions in financial markets are important in the U.S. and the Euro area. Moreover, the size of these frictions is larger in the case of the Euro area. This is in line with independent observations suggesting that financial markets are more developed and integrated in the U.S., and that the institutional and legal framework in the two areas differ. For example, Danthine et al. (1999) argue that the legal differences among European countries, and the lack of a 'European corporate law', constitute an additional factor of market segmentation. These authors claim that the European financial framework is not harmonized when it comes to law, taxation, and supervisory
and regulatory institutions. Evidently, such discrepancies can easily translate into a less efficient credit market.

Moreover, the U.S. has a more fragmented banking sector than the Euro area and a larger number of publicly listed firms 'per capita', which may also imply a more transparent and competitive market.

A number of studies have documented these kinds of differences in financial markets on the two sides of the Atlantic. For instance, Faia (2002) shows the Thomson rating to be lower in the U.S., meaning a more efficient banking system. Moreover, while the return on assets is higher in the U.S., loan losses are lower, which is consistent with the results obtained in my estimation. Her paper shows loan losses to be 0.10 and 0.32 percent in the U.S. and the Euro area, respectively. In the model, these numbers are related to monitoring costs: loan losses are an increasing function of monitoring costs and though, consistent with higher monitoring costs in the Euro area.

The financial market structure can play an important role in the transmission mechanism of shocks and the decisions of firms. The fact that the Euro area presents more frictions in credit markets than the U.S. might generate different dynamics of investment. For example, with the rest of the parameters being equal, a model with larger monitoring costs has a greater response in investment to a monetary policy shock.

Figure 7 and 8 plot the impulse response function to a one standard deviation monetary shock of the benchmark model, with and without monitoring costs, in each of the two areas. In the absence of monitoring costs, both inflation and investment react much less to the shock. To facilitate comparison, Figure 9 shows the impulse response functions to a monetary policy shock of equal size in both economies, evaluated at the posterior mean for the benchmark model. Even though monitoring costs are larger in the Euro area, the response of investment is similar in both economies. In the model, this is due to higher investment adjustment costs in the Euro area, which offset the larger credit
frictions. ${ }^{30}$ In that sense, frictions in credit markets are not a good explanation for the 'output composition puzzle' described in Angeloni et al. (2003). These authors find that while the response patterns to a monetary policy shock are similar in the U.S. and the Euro area, there is a noticeable difference in the composition of output changes. In the U.S., consumption is the predominant driver of output changes after a monetary shock, while in the Euro area it is investment. Figure 9 shows that even though there exist higher financial frictions in the Euro area, this does not imply a different response of output, investment or consumption after a monetary policy shock.

To check that this is not caused by other parameters in the model, I perform a counterfactual analysis. In Figure 10, I plot the impulse response function to a monetary policy shock of the estimated model for the U.S. (evaluated at the mean of the posterior) and the same exercise only changing the value of three parameters: monitoring costs, steady state risk premium and investment adjustment costs. I set these three parameters equal to their mean estimates for the Euro area. The figure suggests that larger monitoring costs in the Euro area are not related to a different response of investment after a monetary policy shock. Moreover, the existence of higher monitoring costs implies a higher response of the costs of funds in the Euro area.

The previous results suggest that the answer why the estimates of financial frictions are higher in the Euro area might be found analyzing the response of the economy to other shocks. Figure 11 shows the same counterfactual exercise as before in the case of a productivity shock. The figure shows that again higher financial frictions are offset by higher capital adjustment costs and investment reacts similarly in both cases. A positive productivity shock increases the marginal productivity of capital and thus the rental price of capital, the return on capital, the demand of capital and the price of capital. This has a positive effect on net worth and with higher financial frictions, these effects are larger through the positive effect on net worth. For instance, the higher price of

[^19]capital under higher financial frictions increases the rental price of capital. Moreover, a positive productivity shock decreases marginal costs given the increase in the marginal productivity of labor and capital. The initial fall in marginal costs is lower when financial frictions are larger since also the increase in the rental price of capital is larger. This difference in marginal costs causes a lower decrease in inflation on impact and in the next periods. This shows that the behavior of inflation and nominal interest rates after a productivity shock can favor a model with higher financial frictions and adjustment costs, even though the path of investment and output is similar in the two scenarios.

Last, Figure 12 shows the impulse response function to a preference shock in the same counterfactual scenario. Now, the model with higher monitoring costs and capital adjustment cost has a lower response of investment. Why is that? In this case, the higher adjustment costs of capital dominate and even if there exists higher financial frictions, investment reacts less. (Given that the capital stock reacts the same in both parametrizations.)

## 6 Conclusions

I study an extended version of the BGG model augmented with other frictions, such as price indexation to past inflation, sticky wages, consumption habits and variable capital utilization. This model is estimated using Bayesian techniques for both the U.S. and the Euro area.

The results indicate that financial frictions are relevant in both areas, but quantitatively more important in the Euro area. This suggests that the financial market structure can play an important role in the transmission mechanism of shocks and the decisions of firms. The fact that the Euro area has more frictions in credit markets might lead one to believe that it has different dynamics in investment as compared to the U.S. In actual fact, however, the response of investment is similar in both economies after most shocks.

In the model, this is due to higher investment adjustment costs in the Euro area, which offset the larger credit frictions. Higher financial frictions in the Euro area do generate different responses of prices, wages and the external risk premium, though.

Future research should investigate the robustness of these results to alternative ways of specifying financial frictions. The financial accelerator mechanism is certainly a popular device to account for informational frictions in financial markets, but not the only one.

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| Parameter | Prior |  |  |  |  | U.S. Posterior |  |  |  |  | Euro Area Posterior |  |  |  |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Type | Mode | St. Er. | $5 \%$ | Median | Mean | $95 \%$ | $\widehat{R}$ | $5 \%$ | Median | Mean | $95 \%$ | $\widehat{R}$ |  |
| $\sigma_{r}$ monetary shock | Gam | 0.01 | 0.005 | 0.003 | 0.004 | 0.004 | 0.004 | 1.002 | 0.002 | 0.002 | 0.002 | 0.003 | 1.035 |  |
| $\sigma_{a}$ technology shock | Gam | 0.01 | 0.005 | 0.006 | 0.007 | 0.007 | 0.008 | 1.002 | 0.007 | 0.008 | 0.008 | 0.009 | 1.000 |  |
| $\sigma_{g}$ gov. spending shock | Gam | 0.01 | 0.005 | 0.015 | 0.017 | 0.017 | 0.019 | 1.000 | 0.015 | 0.017 | 0.017 | 0.019 | 1.001 |  |
| $\sigma_{\nu}$ preferences shock | Gam | 0.10 | 0.05 | 0.089 | 0.126 | 0.126 | 0.165 | 1.024 | 0.082 | 0.164 | 0.155 | 0.218 | 1.793 |  |
| $\sigma_{\xi}$ labor supply shock | Gam | 0.10 | 0.05 | 0.026 | 0.031 | 0.031 | 0.037 | 1.014 | 0.027 | 0.032 | 0.032 | 0.037 | 1.001 |  |
| $\sigma_{\lambda}$ price mark up shock | Gam | 0.10 | 0.05 | 0.271 | 0.327 | 0.329 | 0.397 | 1.021 | 0.272 | 0.318 | 0.320 | 0.376 | 1.019 |  |
| $\sigma_{\tau}$ wage mark up shock | Gam | 0.10 | 0.05 | 1.877 | 2.142 | 2.143 | 2.414 | 1.295 | 1.514 | 1.814 | 1.807 | 2.061 | 1.138 |  |
| $\rho^{r}$ instrument rule | Beta | 0.85 | 0.10 | 0.354 | 0.431 | 0.430 | 0.500 | 1.014 | 0.428 | 0.500 | 0.499 | 0.564 | 1.038 |  |
| $\rho^{a}$ technology shock | Beta | 0.85 | 0.10 | 0.953 | 0.977 | 0.976 | 0.993 | 1.000 | 0.965 | 0.987 | 0.985 | 0.996 | 1.006 |  |
| $\rho^{g}$ gov. spend. shock | Beta | 0.85 | 0.10 | 0.868 | 0.922 | 0.920 | 0.963 | 1.010 | 0.739 | 0.841 | 0.841 | 0.948 | 1.011 |  |
| $\rho^{\nu}$ preferences shock | Beta | 0.85 | 0.10 | 0.991 | 0.994 | 0.993 | 0.996 | 1.008 | 0.993 | 0.997 | 0.996 | 0.998 | 1.572 |  |
| $\rho^{\xi}$ labor supply shock | Beta | 0.85 | 0.10 | 0.985 | 0.993 | 0.992 | 0.998 | 1.002 | 0.99 | 0.996 | 0.995 | 0.999 | 1.000 |  |

[^20]Table 1-B: Prior and Posterior Distribution of the Parameters

| Parameter | Prior |  |  | U.S. Posterior |  |  |  |  | Euro Area Posterior |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Type | Mode | St. Er. | 5\% | Median | Mean | 95\% | $\widehat{R}$ | 5\% | Median | Mean | 95\% | $\widehat{R}$ |
| $\gamma^{\pi}$ inflation in monetary rule | Norm | 1.50 | 0.05 | 1.542 | 1.614 | 1.614 | 1.687 | 1.001 | 1.482 | 1.555 | 1.556 | 1.631 | 1.013 |
| $\gamma^{y}$ output in monetary rule | Norm | 0.50 | 0.05 | 0.157 | 0.240 | 0.240 | 0.322 | 1.001 | 0.146 | 0.227 | 0.227 | 0.307 | 1.015 |
| $\sigma$ risk aversion | Norm | 1.00 | 0.10 | 0.984 | 1.112 | 1.110 | 1.227 | 1.034 | 1.052 | 1.208 | 1.211 | 1.373 | 1.155 |
| $\theta$ prob. of not adj. prices | Beta | 0.70 | 0.05 | 0.758 | 0.782 | 0.782 | 0.804 | 1.013 | 0.812 | 0.833 | 0.832 | 0.852 | 1.007 |
| $\varphi$ elasticity of K price wrt I/K | Unif | -0.5* | 0.29 | -0.578 | -0.471 | -0.475 | -0.386 | 1.001 | -0.999 | -0.980 | -0.973 | -0.92 | 1.000 |
| $\gamma$ entrepreneurs' rate of survival | Beta | . 975 | 0.01 | 0.985 | 0.991 | 0.991 | 0.995 | 1.000 | 0.991 | 0.994 | 0.994 | 0.997 | 1.007 |
| $\mu$ monitoring costs | Beta | 0.12 | 0.05 | 0.083 | 0.118 | 0.119 | 0.158 | 1.000 | 0.117 | 0.184 | 0.182 | 0.245 | 1.005 |
| $r^{k}-r$ ss risk premium | Gam | 0.005 | 0.002 | 0.004 | 0.006 | 0.006 | 0.008 | 1.000 | 0.006 | 0.009 | 0.009 | 0.012 | 1.005 |
| $\vartheta$ prob. of not adj. wages | Beta | 0.70 | 0.05 | 0.174 | 0.207 | 0.208 | 0.243 | 1.171 | 0.236 | 0.274 | 0.274 | 0.311 | 1.058 |
| $h$ habit formation | Beta | 0.70 | 0.05 | 0.548 | 0.605 | 0.604 | 0.659 | 1.004 | 0.458 | 0.516 | 0.516 | 0.574 | 1.068 |
| $\delta^{\prime \prime} / \delta^{\prime}$ variable dep. parameter | Gam | 1.00 | 0.05 | 0.939 | 1.018 | 1.020 | 1.106 | 1.098 | 0.913 | 0.996 | 0.997 | 1.087 | 1.301 |

Note: Benchmark model with financial accelerator (FA).

Table 2-A: Robustness and Different Models Performance - Mean of the Posterior distribution for U.S. Data | Parameter | BGG Model |  | Pr. Indexation |  | Sticky Wages |  | Cons. Habits |  | Benchmark |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | FA | no FA | FA | no FA | FA | no FA | FA | no FA | FA | No FA |
| $\sigma_{r}$ monetary shock | 0.003 | 0.007 | 0.004 | 0.006 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 |
| $\sigma_{a}$ technology shock | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.007 | 0.006 |
| $\sigma_{g}$ gov. spending shock | 0.015 | 0.019 | 0.016 | 0.019 | 0.016 | 0.019 | 0.016 | 0.019 | 0.017 | 0.019 |
| $\sigma_{\nu}$ preferences shock | 0.009 | 0.107 | 0.075 | 0.077 | 0.123 | 0.117 | 0.135 | 0.147 | 0.126 | 0.145 |
| $\sigma_{\xi}$ labor supply shock | 0.011 | 0.023 | 0.020 | 0.027 | 0.027 | 0.033 | 0.037 | 0.046 | 0.031 | 0.040 |
| $\sigma_{\lambda}$ price mark up shock | 0.245 | 0.148 | 0.175 | 0.151 | 0.289 | 0.219 | 0.335 | 0.236 | 0.329 | 0.260 |
| $\sigma_{\tau}$ wage mark up shock | 0.487 | 0.679 | 0.583 | 0.762 | 1.850 | 2.112 | 1.995 | 2.262 | 2.143 | 2.438 |
| $\rho^{r}$ instrument rule | 0.193 | 0.135 | 0.218 | 0.101 | 0.359 | 0.279 | 0.409 | 0.345 | 0.430 | 0.395 |
| $\rho^{a}$ technology shock | 0.822 | 0.807 | 0.993 | 0.978 | 0.971 | 0.889 | 0.981 | 0.971 | 0.976 | 0.923 |
| $\rho^{g}$ gov. spend. shock | 0.909 | 0.951 | 0.916 | 0.933 | 0.931 | 0.958 | 0.944 | 0.968 | 0.920 | 0.966 |
| $\rho^{\nu}$ preferences shock | 0.898 | 0.996 | 0.993 | 0.995 | 0.995 | 0.995 | 0.993 | 0.993 | 0.993 | 0.994 |
| $\rho^{\xi}$ labor supply shock | 0.947 | 0.955 | 0.960 | 0.932 | 0.967 | 0.947 | 0.991 | 0.987 | 0.992 | 0.989 |

I cumulatively add price indexation, sticky wages, consumption habits and variable capital utilization. This last model
corresponds to the benchmark model. In all these cases, I estimate the model with (FA) and without financial accelerator (no FA).
Table 2-B: Robustness and Different Models Performance - Mean of the Posterior distribution for U.S. Data

| Parameter | BGG Model |  | Pr. Indexation |  | Sticky |  | Wages | Cons. Habits |  | Benchmark |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | FA | no FA | FA | no FA | FA | no FA | FA | no FA | FA | No FA |  |
| $\gamma^{\pi}$ inflation in monetary rule | 1.287 | 1.719 | 1.502 | 1.636 | 1.607 | 1.615 | 1.623 | 1.631 | 1.614 | 1.637 |  |
| $\gamma^{y}$ output in monetary rule | 0.140 | 0.061 | 0.275 | 0.221 | 0.231 | 0.180 | 0.220 | 0.221 | 0.240 | 0.198 |  |
| $\sigma$ risk aversion | 1.134 | 1.227 | 1.330 | 1.288 | 1.322 | 1.312 | 1.144 | 1.158 | 1.110 | 1.100 |  |
| $\theta$ prob. of not adj. prices | 0.700 | 0.710 | 0.637 | 0.675 | 0.757 | 0.732 | 0.779 | 0.747 | 0.782 | 0.759 |  |
| $\varphi$ elasticity of K price wrt I/K | -0.100 | -0.078 | -0.142 | -0.060 | -0.361 | -0.139 | -0.370 | -0.217 | -0.475 | -0.220 |  |
| $\gamma$ entrepreneurs' rate of survival | 0.989 | 0.972 | 0.992 | 0.971 | 0.992 | 0.972 | 0.989 | 0.971 | 0.991 | 0.971 |  |
| $\mu$ monitoring costs | 0.222 | - | 0.191 | - | 0.121 | - | 0.099 | - | 0.119 | - |  |
| $r^{k}-r$ steady state risk premium | 0.012 | - | 0.010 | - | 0.006 | - | 0.005 | - | 0.006 | - |  |
| $\vartheta$ prob. of not adj. wages | - | - | - | - | 0.181 | 0.162 | 0.218 | 0.191 | 0.208 | 0.186 |  |
| $h$ habit formation | - | - | - | - | - | - | 0.601 | 0.653 | 0.604 | 0.661 |  |
| $\delta^{\prime \prime} / \delta^{\prime}$ variable dep. parameter | - | - | - | - | - | - | - | - | 1.020 | 1.005 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
| Log Marginal Data Density | 1941.2 | 1819.9 | 1927.9 | 1860.9 | 1858.7 | 1803.6 | 1876.9 | 1827.5 | 1880.2 | 1829.8 |  |
| Log Bayes Factor | 0 | 121.3 | 0 | 67.0 | 0 | 55.1 | 0 | 49.3 | 0 | 50.5 |  |
| Bayes Factor | 1 | $1 \mathrm{e}+52$ | 1 | $1 \mathrm{e}+29$ | 1 | $1 \mathrm{e}+23$ | 1 | $1 \mathrm{e}+21$ | 1 | $1 \mathrm{e}+21$ |  |

Note: The first two columns represent the standard BGG model with and without financial accelerator. In the next columns,
I cumulatively add price indexation, sticky wages, consumption habits and variable capital utilization. This last model
corresponds to the benchmark model. In all these cases, I estimate the model with (FA) and without financial accelerator (no FA).

Table 3-A: Robustness and Different Models Performance - Mean of the Posterior distribution for European Data | Parameter | BGG Model |  | Pr. Indexation |  | Sticky Wages |  | Cons. Habits |  | Benchmark |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | FA | no FA | FA | no FA | FA | no FA | FA | no FA | FA | no FA |
| $\sigma_{r}$ monetary shock | 0.002 | 0.006 | 0.002 | 0.004 | 0.002 | 0.003 | 0.002 | 0.003 | 0.002 | 0.003 |
| $\sigma_{a}$ technology shock | 0.007 | 0.007 | 0.007 | 0.008 | 0.007 | 0.007 | 0.007 | 0.007 | 0.008 | 0.008 |
| $\sigma_{g}$ gov. spending shock | 0.017 | 0.016 | 0.016 | 0.016 | 0.017 | 0.016 | 0.017 | 0.016 | 0.017 | 0.016 |
| $\sigma_{\nu}$ preferences shock | 0.012 | 0.101 | 0.039 | 0.08 | 0.060 | 0.100 | 0.078 | 0.133 | 0.155 | 0.104 |
| $\sigma_{\xi}$ labor supply shock | 0.022 | 0.022 | 0.022 | 0.025 | 0.017 | 0.022 | 0.031 | 0.037 | 0.032 | 0.033 |
| $\sigma_{\lambda}$ price mark up shock | 0.347 | 0.285 | 0.203 | 0.166 | 0.301 | 0.245 | 0.314 | 0.223 | 0.320 | 0.252 |
| $\sigma_{\tau}$ wage mark up shock | 0.298 | 0.510 | 0.368 | 0.547 | 1.660 | 2.166 | 1.713 | 2.116 | 1.807 | 2.369 |
| $\rho^{r}$ instrument rule | 0.371 | 0.146 | 0.342 | 0.169 | 0.530 | 0.331 | 0.468 | 0.384 | 0.499 | 0.395 |
| $\rho^{a}$ technology shock | 0.975 | 0.93 | 0.989 | 0.994 | 0.896 | 0.831 | 0.987 | 0.939 | 0.985 | 0.842 |
| $\rho^{g}$ gov. spend. shock | 0.903 | 0.967 | 0.899 | 0.967 | 0.828 | 0.958 | 0.937 | 0.969 | 0.841 | 0.965 |
| $\rho^{\nu}$ preferences shock | 0.943 | 0.996 | 0.983 | 0.997 | 0.988 | 0.995 | 0.992 | 0.995 | 0.996 | 0.994 |
| $\rho^{\xi}$ labor supply shock | 0.981 | 0.973 | 0.984 | 0.974 | 0.992 | 0.977 | 0.995 | 0.992 | 0.995 | 0.994 |

I cumulatively add price indexation, sticky wages, consumption habits and variable capital utilization. This last model
corresponds to the benchmark model. In all these cases, I estimate the model with (FA) and without financial accelerator (no FA).
Table 3-B: Robustness and Different Models Performance - Mean of the Posterior distribution for European Data

| Parameter | BGG Model FA no FA |  | Pr. Indexation |  | Sticky Wages FA no FA |  | Cons. Habits <br> FA no FA |  | Benchmark |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\gamma^{\pi}$ inflation in monetary rule | 1.501 | 1.713 | 1.565 | 1.639 | 1.506 | 1.539 | 1.558 | 1.617 | 1.556 | 1.568 |
| $\gamma^{y}$ output in monetary rule | 0.285 | 0.146 | 0.309 | 0.239 | 0.261 | 0.120 | 0.217 | 0.191 | 0.227 | 0.152 |
| $\sigma$ risk aversion | 1.264 | 1.279 | 1.317 | 1.310 | 1.157 | 1.223 | 1.180 | 1.135 | 1.211 | 1.093 |
| $\theta$ prob. of not adj. prices | 0.772 | 0.768 | 0.736 | 0.757 | 0.806 | 0.839 | 0.826 | 0.827 | 0.832 | 0.843 |
| $\varphi$ elasticity of K price wrt I/K | -0.469 | -0.331 | -0.317 | -0.171 | -0.806 | -0.275 | -0.619 | -0.461 | -0.973 | -0.347 |
| $\gamma$ entrepreneurs' rate of survival | 0.995 | 0.972 | 0.994 | 0.972 | 0.997 | 0.972 | 0.994 | 0.972 | 0.994 | 0.971 |
| $\mu$ monitoring costs | 0.243 | - | 0.314 | - | 0.520 | - | 0.129 | - | 0.182 | - |
| $r^{k}-r$ steady state risk premium | 0.011 | - | 0.014 | - | 0.023 | - | 0.006 | - | 0.009 | - |
| $\vartheta$ prob. of not adj. wages | - | - | - | - | 0.271 | 0.240 | 0.254 | 0.236 | 0.274 | 0.245 |
| $h$ habit formation | - | - | - | - | - | - | 0.495 | 0.573 | 0.516 | 0.569 |
| $\delta^{\prime \prime} / \delta^{\prime}$ variable dep. parameter | - | - | - | - | - | - | - | - | 0.997 | 1.013 |
| Log Marginal Data Density | 1898.0 | 1773.9 | 1927.6 | 1904.9 | 1920.8 | 1882.0 | 1902.6 | 1891.3 | 1921.0 | 1881.1 |
| Log Bayes Factor | 0 | 124.1 | 0 | 22.6 | 0 | 38.9 | 0 | 11.2 | 0 | 39.9 |
| Bayes Factor | 1 | $1 \mathrm{e}+53$ | 1 | $1 \mathrm{e}+9$ | 1 | $1 \mathrm{e}+16$ | 1 | $1 \mathrm{e}+4$ | 1 | $1 \mathrm{e}+17$ |

Note: The first two columns represent the standard BGG model with and without financial accelerator. In the next columns,
I cumulatively add price indexation, sticky wages, consumption habits and variable capital utilization. This last model
corresponds to the benchmark model. In all these cases, I estimate the model with (FA) and without financial accelerator (no FA).




Figure 4: Prior and posterior distribution of the benchmark model with financial frictions for Euro data.


$\begin{array}{llllll}-0.5 & 1980 & 1985 & 1990 & 1995 & 2000 \\ & & & 2005 \\ & & \text { Nominal Int. Rate }\end{array}$


Figure 5: U.S. actual and one-side Kalman filter fitted data evaluated at the mean of the posterior. Thin solid line - benchmark model
with financial accelerator. Dashed line - benchmark model without financial accelerator. Thick solid line - Actual data.

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Figure 6: European actual and one-side Kalman filter fitted data evaluated at the mean of the posterior. Thin solid line - benchmark
model with financial accelerator. Dashed line - benchmark model without financial accelerator. Thick solid line - Actual data.




Figure 7: Impulse Response Function to a one standard deviation monetary policy shock (mean, 5 and 95 percentiles). Solid line:
benchmark financial accelerator model. Dashed line: benchmark model without financial accelerator. Values expressed as percentage
deviation from steady state values, and in the case of inflation and the nominal interest rate as annual percentage points.

European Data


Figure 8: Impulse Response Function to a one standard deviation monetary policy shock (mean, 5 and 95 percentiles). Solid line:

deviation from steady state values, and in the case of inflation and the nominal interest rate as annual percentage points.

Figure 9: Impulse Response functions to a one percent shock to the nominal interest rate (annual) for the benchmark model with
monitoring costs. Solid line: U.S. data. Doted line: European data. Values expressed as percentage deviation from steady state values,
and in the case of inflation, the nominal interest rate and premium as annual percentage points.

Figure 10: Counterfactual: Impulse Response functions to a one percent shock to the nominal interest rate (annual) for the benchmark
model with monitoring costs. Solid line: U.S. data. Star line: U.S. data using credit market frictions and investment adjustment costs
as in the Euro area. Values expressed as percentage deviation from steady state values, and in the case of inflation. the nominal interest
rate and premium as annual percentage points.


Figure 11: Counterfactual: Impulse Response functions to a one standard deviation shock to productivity for the benchmark model with
monitoring costs. Solid line: U.S. data. Star line: U.S. data using credit market frictions and investment adjustment costs as in the
Euro area. Values expressed as percentage deviation from steady state values, and in the case of inflation, the nominal interest rate and
premium as annual percentage points.

Figure 12: Counterfactual: Impulse Response functions to a one standard deviation preference shock for the benchmark model with
monitoring costs. Solid line: U.S. data. Star line: U.S. data using credit market frictions and investment adjustment costs as in the
Euro area. Values expressed as percentage deviation from steady state values, and in the case of inflation, the nominal interest rate and
premium as annual percentage points.


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[^1]:    ${ }^{1}$ There exists a large literature emphasizing the role of financial frictions in business cycles, see Kiyotaki and Moore (1997), Greenwald and Stiglitz (1993).
    ${ }^{2}$ However, the effects of the financial accelerator on output may depend on the policy rule and the type of shock.

[^2]:    ${ }^{3}$ They estimate the model in BGG where the structural parameters that underpin the financial contract are reduced to the elasticity of the external finance premium with respect to the change in the leverage position of entrepreneurs. In that sense, they are not able to identify monitoring costs or other structural parameters regarding financial frictions.
    ${ }^{4}$ However, they focus only on the propagation of monetary policy shocks.

[^3]:    ${ }^{5}$ Moreover, and differently from Christensen and Dib (2004) and Meier and Muller (2005) I estimate a more complex model and I am able to identify the structural parameters of the financial contract.

[^4]:    ${ }^{6}$ Even if I include financial intermediaries in my model, Christiano et al. (2003) consider a larger banking sector which manages different kinds of deposits and loans, and requires capital and labor services.

[^5]:    ${ }^{7}$ We can assume that capital-producing firms are owned by entrepreneurs. After entrepreneurs rebuy the old stock of capital, used capital depreciates.
    ${ }^{8} u_{t}$ can take any value $\geq 0$, where values greater than one mean that there exists over utilization of capital.
    ${ }^{9}$ One example of this kind of function can be $\delta\left(u_{t}\right)=1-\frac{1+p}{p+\exp ^{\varepsilon u_{t}}}$ with $p, \varepsilon>0$. In this case, $\delta(0)=0$, $\delta(\infty)=1, \delta(1)=1-\frac{1+p}{p+\exp ^{\varepsilon}}=\delta$. However, I focus on a more general case of functional forms and I estimate $\delta_{s s}^{\prime \prime} / \delta_{s s}^{\prime}$.

[^6]:    ${ }^{10}$ As in Christiano et al. (2003), I assume that after entrepreneurs purchase capital, they draw an idiosyncratic shock which changes $\widetilde{k}_{t+1}^{i}$ to $\omega_{t+1}^{i} \widetilde{k}_{t+1}^{i}$.
    ${ }^{11}$ The relevant price of capital at the end of period $t$ is $q_{t}$.

[^7]:    ${ }^{12}$ Levin et al. (2004) estimate $\mu$ to be time varying.
    ${ }^{13}$ The relevant price here is $q_{t}$ since capital price gains are included in $r_{t+1}^{k}$.
    ${ }^{14}$ The derivation of these conditions can be provided by the author upon request.

[^8]:    ${ }^{15}$ So in average entrepreneurs live $1 /(1-\gamma)$ periods.
    ${ }^{16}$ This approach has been used by Baxter and Farr (2001), among others.

[^9]:    ${ }^{17} \mathrm{I}$ assume the government adjust the fiscal effects of monetary policy with lump sum taxes.
    ${ }^{18}$ The last term is the loss in monitoring costs associated with defaulting entrepreneurs.

[^10]:    ${ }^{19}$ This is the same notation as in Christiano et al. (2005) but a wage mark up has been introduced and the mark up is in net terms.

[^11]:    ${ }^{20}$ In the model without financial frictions, $\mu=0$, and these equations and the law of motion of net worth are:

    $$
    \begin{gathered}
    E_{t} \widehat{r}_{t+1}^{k}=\widehat{r}_{t} \\
    {[(1-F(\varpi))] \frac{\widetilde{K}}{N} \varpi \widehat{\varpi}_{t+1}+\left[\frac{\widetilde{K}-N}{N}\right]\left(\widehat{r}_{t+1}^{k}-\widehat{r}_{t}\right)=\widehat{\widetilde{k}}_{t+1}+\widehat{q}_{t}-\widehat{n}_{t+1},}
    \end{gathered}
    $$

[^12]:    ${ }^{21}$ Another difference is that in the original BGG model, there are only three shocks affecting the economy: monetary policy, government and technology shocks. Moreover, the interest rate rule only responds to past inflation which has strong implications regarding the propagation of shocks.

[^13]:    ${ }^{22}$ Since this number does not include transfers, we can assume the same value for the U.S. and the Euro area
    ${ }^{23}$ In models with a financial accelerator, these ratios will also depend on the risk premium.

[^14]:    ${ }^{24}$ I do not include any financial variables since to compare the model with and the one without financial frictions, the first will present a natural advantage in the case when these variables are included.
    ${ }^{25}$ U.S. data was taken from the Bureau of Economic Analysis of the U.S. Department of Commerce (BEA), the IMF database and the Bureau of Labor Statistics (BLS). Real output is measured by real GDP converted into per capita terms dividing by the population aged above sixteen (P16). Real consumption is real personal consumption expenditures divided by P16. Real investment is real gross private domestic investment also in per capita terms. Hours worked are measured by the product of average weekly hours in the private sector times the population aged above twenty. The nominal interest rate is the Federal Funds Rate, and inflation is calculated as the difference of the GDP deflator. Real wages are measured by the average hourly earnings of production workers in real terms. All series were detrended with a linear trend and in the case of the interest rate, I used the same trend as inflation.

[^15]:    ${ }^{26}$ European data was taken from the AWM database of the ECB. Real output is measured by real GDP converted into per capita terms dividing by the labor force. Real consumption is real consumption divided by the labor force. Real investment is real gross investment also in per capita terms. To calculate hours worked, I use data on total employment, and transform it into hours worked using the same criterion as Smets and Wouters (2003). They assume that in any period, only a constant fraction of firms, $\xi_{e}$, is able to adjust employment to its desired total labor input. This results in the following equation for employment:

    $$
    \widehat{e}_{t}=\beta \widehat{e}_{t+1}+\frac{\left(1-\xi_{e}\right)\left(1-\beta \xi_{e}\right)}{\xi_{e}}\left(\widehat{l}_{t}-\widehat{e}_{t}\right)
    $$

    where $\widehat{e}_{t}$ is total employment. In contrast to them, I do not estimate $\xi_{e}$, but following their results and the results in Adolfson et al. (2004), I fix it equal to 0.70 . The nominal interest rate is the quarterly short-term interest rate, and inflation is calculated as the difference of the GDP deflator. Real wages are measured by the wage rate deflated by the GDP deflator. All series were detrended with a linear trend and in the case of the interest rate, I used the same trend as inflation.

[^16]:    ${ }^{27}$ For instance, for given parameters, a model with financial frictions displays a lower response of prices after a technology shock. Similarly, a lower response of prices occurs when we introduce variable capital utilization, since it offsets the fluctuations in labor productivity and affects the marginal cost.

[^17]:    ${ }^{28}$ These values imply an elasticity of the external finance premium with respect to the leverage ratio of 0.04 , which is lower than the value estimated by Christensen and Dib (2004) but close to the 0.05 used in BGG. The implied standard deviation of the idiosyncratic shock, $\sigma_{\omega}$, is 0.13 .

[^18]:    ${ }^{29}$ In the case of models without financial frictions, introducing variable capital utilization decreases the marginal data density. This result is in line with Adolfson et al. (2004), who find that a model without variable capital utilization delivers a higher marginal density for European data.

[^19]:    ${ }^{30}$ de Walque et al. (2005) also find that adjustment costs in capital accumulation are larger in the Euro area.

[^20]:    Note: Benchmark model with financial accelerator (FA).

